

Dynamic Coefficient β Curve Determination

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1. Introduction

The response spectral theory, introduced by Biot in 1934, has become a cornerstone in seismic analysis and structural engineering. This theory provides a framework for determining the magnitude of seismic actions and analyzing the seismic response of structures. Biot's approach considers the distribution of mass and the vibration modes of buildings, which vary with height, to accurately assess seismic impacts. In seismic design, the dynamic coefficient β curve plays a critical role in quantifying the seismic forces that structures must withstand [1] [2] [3]. This curve is integral to the development of aseismic design standards, as it reflects the relationship between the maximum absolute acceleration response and the ground acceleration in a singledegree-of-freedom system. The β curve is influenced by various factors, including the natural vibration period of the structure and the geographic characteristics of the site. Despite its importance, the determination of the dynamic coefficient β curve requires careful consideration of several parameters, such as the excellent period of seismic waves, the design value of the dynamic coefficient, and the acceleration response spectrum [4] [5] [6]. This study aims to refine the β curve model by integrating statistical analysis with empirical seismic data, thereby enhancing its applicability in modern aseismic design standards. Our research focuses on the descent interval, branch points, and the acceleration response spectrum, particularly for cases where the natural vibration period T equals 10 seconds. By improving the β curve's accuracy and reliability, we contribute to

advancing seismic design practices and ensuring the structural resilience of buildings in earthquake-prone areas [7] [8] [9].

$$
F_{ji} = K_E \cdot \beta_j \cdot \eta_{ji} \cdot G_i \tag{1}
$$

Fji -seismic action at the ith point in the j-difference vibration shape

KE - seismic activity control coefficient

βj -Dynamic coefficients along the jth vibration

ηji - vibration shape coefficients at the ith mass in the j-difference vibration shape

Gi - ith mass's weight

In the equation 1, $β$ is taken on the dynamic coefficient $β$ curve.

KE is a factor that guarantees the strength of an earthquake that can be encountered on the site, which depends on the geographic features of the area and is specified differently from country to country.

The vibration shape coefficient ηji is calculated as follows:

$$
\eta_{ji} = X_{ji} \sum_{i=1}^{n} X_{ji} G_i / \sum_{i=1}^{n} X_{ji}^2 G_i
$$
 (2)

Xji-the relative horizontal displacement of the ith mass in the jth natural vibration shape

Thus, ηji is unintentionally determined according to the dynamic properties of the structure.

β obtains a statistical value of the ratio of the maximum absolute acceleration response and ground acceleration of the single-degree-of-freedom system, which is defined and written differently from country to country.

The dynamical coefficient β curve reflected in the aseismic design standard of our country is the same as Fig 1. Here the maximum value of the acceleration response spectrum β max=2.3 . ([1])

Figure 1 the β curve reflected in aseismic design standard

In Fig. 1, Tg is the exellent period of the base, T is the natural vibration period of the structure.

The Aseismic Design Standards (GB 5011-2010) of the People's Republic of China uses the seismic influence coefficient curve multiplied by the seismic action adjustment factor KE to the acceleration response spectral value β, as Equation 3 (GB 5011-2010), which is essentially the same as the accelerometer response spectral curve in nature because KE is a constant value according to the type of construction site. [2].

$$
\alpha = KE \cdot \beta \tag{3}
$$

Figure 2 The seismic influence coefficient α curve of the Chinese aseismic design standard

The damping index γ of the curve descent step is as follows:

$$
\gamma = 0.9 + \frac{0.05 - \zeta}{0.3 + 6\zeta}
$$
\n(4)

The slope adjustment coefficient η1 of the straight-down step is determined as the following.

$$
\eta_1 = 0.02 + \frac{0.05 - \zeta}{4 + 32\zeta} \tag{5}
$$

The attenuation coefficient η2 is defined as the following.

$$
\eta_2 = 1 + \frac{0.05 - \zeta}{0.08 + 1.6\zeta}
$$
\n(6)

In GB 5011-2010, βmax is 2.25. [2]

In Fig. 2, Tg is the exellent period of the base, T is the natural vibration period of the structure.

As the dynamic coefficient β curve of ASCE 7 is shown in Fig 3, the β curve in the long period interval, T>TL, descends to the exponential form of 1/T2. (The maximum is divided into five groups of 4, 6, 8, 12, and 16 s according to the site category) [2].

Figure 3 The β curve of ASCE 7

2. Method

This study involves collecting seismic data from various sources, including historical earthquake records and accelerometer data. Fourier transform analysis is employed to determine the excellent period of seismic waves, identifying the period at which the power spectrum peaks. The dynamic coefficient β curve is analyzed by initially estimating parameters through statistical analysis of the maximum absolute acceleration response and ground acceleration. The model is refined by fitting empirical data to a theoretical curve, validated against existing seismic standards. Statistical analysis assesses the distribution of βmax values, and sensitivity analysis validates the model by examining the effects of varying natural vibration periods and damping ratios. This methodology provides a

rigorous framework for determining the dynamic coefficient β curve, enhancing its applicability in modern seismic design standards.

3. Result and Discussion

The seismic response and acceleration response spectra of singe-degree-of-freedom systems

To enhance and expand the theoretical discussion related to the provided sentences, consider the following revision: The seismic response of a single-degree-of-freedom (SDOF) system is a foundational aspect of aseismic design and analysis. This is because the SDOF system's seismic response serves as a fundamental model for understanding the behavior of more complex structural systems during seismic events [10] [11] [12]. The dynamic coefficient curve, which corresponds to the acceleration response spectrum of the SDOF system, is crucial in quantifying the magnitude of seismic actions in response spectral analysis. This curve provides insights into the maximum expected ground acceleration and helps in designing structures that can withstand seismic forces effectively. By accurately determining the parameters of the dynamic coefficient β curve, including the excellent period of seismic waves and the descent interval, engineers can enhance the reliability and safety of buildings. This study advances the understanding of the β curve by integrating empirical seismic data with theoretical modeling, ensuring its applicability in modern seismic design standards and contributing to the development of resilient infrastructure.

When an earthquake is encountered in a free diagram such as a in Fig. 4, it oscillates like the b of Fig. 4.

Figure 4 The vibration of a single-degree system

Then the absolute displacement Y(t) of the mass m, consists of a rigid-body displacement $y_g(t)$ along the basis and of a displacement y(t) of the mass m, i.e., the sum of the relative displacement to the base, which occurs when the structure is elastic.

Let's establish the vibration equation of the system.

The working forces of the system are resilience $ky(t)$, resistivity $\phi(y(t))$ and inertia forces $m[y_s(t) + \ddot{y}(t)]$, and these are balanced.

Establishing the equilibrium equation is as follows.

$$
-m[\ddot{y}_g(t) + \ddot{y}(t)] - ky(t) - c\dot{y}(t) = 0
$$
\n(7)

$$
m\ddot{y}(t) + ky(t) + c\dot{y}(t) = -m\ddot{y}_g(t)
$$
\n⁽⁸⁾

$$
\omega^2 = \frac{k}{m}, \quad \zeta = \frac{c}{2\sqrt{km}} = \frac{c}{2\omega m} \tag{9}
$$

Eq 1 is the following:.

$$
\ddot{y}(t) + 2\zeta \omega \dot{y}(t) + \omega^2 y(t) = -\ddot{y}_g(t)
$$
\n(10)

The general solution of Eq. (10) consists of the general solution of the corresponding homogeneous equation and the sum of the specific solutions of the non-homogeneous equation and becomes as follows.

$$
y(t) = e^{-\zeta \omega t} \left[y(0) \cos \omega' t + \frac{\dot{y}(0) + \zeta \omega y(0)}{\omega'} \sin \omega' t \right] -
$$

$$
- \frac{1}{\omega'} \int_{0}^{t} \dot{y}(\tau) e^{-\zeta \omega(t-\tau)} \sin \omega'(t-\tau) d\tau
$$
(11)

In Eq. (11), ω' is the eigen frequency of the one-degree-of-freedom system with attenuation and has the following relation to the eigen frequency ω without attenuation.

$$
\omega' = \sqrt{1 - \zeta^2} \omega \tag{12}
$$

The damping ratio of the concrete material is 0.05, which is $\omega' = 0.9987 \omega \approx \omega$.

Also $y(0)$ and y are the initial displacement and initial velocity at t=0.

In general, the initial displacement and initial velocity of the building before an earthquake occur are considered to be 0, so in Eq. (11), the first term becomes 0, and the displacement response of the one-degree system is represented by the afterward harbour.

The derivative $\dot{y}(t)$ of y(t) is the velocity response to the ground and can be written as follows:

$$
\dot{y}(t) = \frac{dy(t)}{d(t)} = -\int_{0}^{t} \ddot{y}_g(\tau) e^{-\xi \omega(t-\tau)} \cos \omega'(t-\tau) d\tau + \frac{\xi \omega}{\omega'} \int_{0}^{t} \ddot{y}_g(\tau) e^{-\xi \omega(t-\tau)} \sin \omega'(t-\tau) d\tau
$$
\n(13)

Substituting Equation (12) and (13) to Equation (10), the absolute acceleration of the system can be found as follows.

$$
\ddot{y}(t) + \ddot{y}_g(t) = -2\zeta \omega \dot{y}(t) - \omega^2 y(t) =
$$
\n
$$
= 2\zeta \omega \int_0^t \ddot{y}_g(\tau) e^{-\zeta \omega(t-\tau)} \cos \omega'(t-\tau) d\tau -
$$
\n
$$
- \frac{2\zeta^2 \omega^2}{\omega'} \int_0^t \ddot{y}_g(\tau) e^{-\zeta \omega(t-\tau)} \sin \omega'(t-\tau) d\tau +
$$
\n
$$
+ \frac{\omega^2}{\omega'} \int_0^t \ddot{y}_g(\tau) e^{-\zeta \omega(t-\tau)} \sin(t-\tau) d\tau
$$
\n(14)

The seismic response is obtained by Equation (11), (13), (14).

However, the recording $\ddot{y}_g(t)$ of the ground acceleration is a random process and cannot be expressed as a function, so the seismic response can be obtained only by numerical integration.

Now let us simply try Equation (14) with

$$
S_a = \left| \ddot{y}(t) + \ddot{y}_g(t) \right|_{\text{max}} \tag{15}
$$

Here.

Sa-The maximum absolute acceleration response of the SDOF system

① The damping ratio ζ is very small (0.05 for concrete material, 0.02 for steel material), neglecting the ζand ² terms in the expressions.

$$
(2). \, \omega' = \omega
$$

sin(t-τ) and cos(t-τ) have the same maximum value as the phase difference is $\pi/2$.

Then, S

 $=\omega \int_{0}^{t} y_g(\tau) e^{-\zeta \omega(t-\tau)} \sin \omega(t-\tau) d\tau$ $S_a = |\ddot{y}(t) + \ddot{y}_g(t)|_{\text{max}} =$ $\omega \left(\ddot{y}_e(\tau) e^{-\zeta \omega(t-\tau)} \sin \omega(t-\tau) d\tau \right)$ (16)

The inertia force in a free-conductor system is then influenced by an earthquake on the structure, and the magnitude of the seismic action is as follows.

$$
F = |F(t)|_{\text{max}} = mS_a = m|\ddot{y}(t) + \ddot{y}_g(t)|_{\text{max}} =
$$

$$
= mg \frac{S_a}{|\ddot{y}_g(t)|} \cdot \frac{|\ddot{y}_g(t)|}{g} = K_E \cdot \beta \cdot G
$$
(17)

 $G = mg$: mass weight

$$
\beta = \frac{S_a}{\left| \ddot{y}_g(t) \right|_{\text{max}}} \tag{18}
$$

β– Dynamic coefficient

KE – seismic activity control coefficient

g y t $K_E = \frac{|y_g|}{|g_g|}$ $E = \frac{\left| \ddot{y}_g(t) \right|_{\text{max}}}{\sqrt{2\pi} \sqrt{2\pi}}$ = (19)

Now if $\omega = 2\pi/T$ is placed in Equation (18), then the following is:

⁼

$$
\beta = \frac{S_a}{\left|\ddot{y}_g(t)\right|_{\text{max}}} =
$$
\n
$$
= \frac{2\pi}{T} \cdot \frac{1}{\left|\ddot{y}_g(t)\right|_{\text{max}}} \left|\int_0^t \ddot{y}_g(\tau) e^{-\zeta \frac{2\pi}{T}(t-\tau)} \sin \frac{2\pi}{T} (t-\tau) d\tau \right|_{\text{max}} \tag{20}
$$

β is the maximum absolute acceleration response, calculated as Sa, and given the damping ratio ζ of the ground acceleration recording and structural material, we can calculate the dynamical coefficient p for different natural vibration periods T by Eq. (20).

The shape of the β-T curve is in perfect agreement with the acceleration response spectral curve, but the only other point is that the longitudinal coordinate value is dimensionless.

The determination of βmax

In the β-T curve, βmax finds the mean value in the interval with the maximum value of the acceleration response spectral curve based on the concrete material $(\zeta=0.05)$.[3]

$$
\beta_{\max} = \overline{\beta}(T) = \frac{\sum_{i=1}^{n} \beta_i(T)|_{\varsigma = 0.05}}{n}
$$
\n(21)

From Fig. 1 to 3, it can be seen that β increases sharply from T=0 s to some small period (0.1 s in Fig, 1, 2) and then reaches the max, and again decreases sharply from the point of its exellent period.

Value determination of β when T=0s

If we look at Eq. 20, we can't get it because β is infinite when T=0 s.

Therefore, in the actual calculation, the calculated value of β is calculated at a very small value of about T=0.05 s.

So what is the β when T = 0 s strictly?

 $T = 0$ s means that the structure becomes rigid and does not oscillate at all.

In this case, the acceleration response by the ground acceleration does not extend.

Because the structure does not oscillate at all, the input acceleration value is the output acceleration value.

That is, $\beta = 1.0$.

Determination of the minimum value of the natural vibration period of the structure reaching βmax

The determination of the dynamic coefficient β curve is crucial in understanding seismic responses. It has been previously confirmed that β equals 1.0 when the natural vibration period T = 0 seconds [13] [14]. Although some β-T curves inaccurately equate β at $T = 0$ with βmax, it is essential to recognize that the acceleration response typically reaches βmax when T is relatively small. Initially, β is assumed to have a value of βmax and remains constant until the excellent period T_g , after which it descends following a hyperbolic function. However, most countries' aseismic design standards specify a minimum natural vibration period T at which β reaches βmax, as illustrated in Figures 1-3. It is important to note that β is a random variable in the β-T curve, leading to significant variability. This study's statistical analysis reveals that the mean and standard deviation of the minimum T value at the first peak point, where β increases and then sharply declines, are 0.1127 and 0.0351, respectively. This analysis supports the scientific determination of a minimum T value of 0.1 seconds for the β-T curve, ensuring safety in seismic action magnitude assessments.

In the present study, the statistical analysis of the value of T of the first peak point, where β grows continuously and declines sharply, shows that the mathematical means and standard deviations of the minimum value of T are 0.1127 and 0.0351.

Drawing a column diagram for estimating the probability density function from 0.04 to 0.51 with a class size of 0.02 is the same as Fig. 5.

Figure 5 Minimum column diagram of the natural vibration period of the structure reaching βmax

The figure shows that in the very β -T curve, β is highly irregular, with very difficulty in defining the minimum distribution of a rapidly rising T.

According to the values of Fig. 5 and the calculated results, it can be seen that it is scientific to see the minimum value of T in the β-T curve to be 0.1 s, and that it gives a safe value even in the determination of the magnitude of seismic action.

Thus, in this study, we propose to use 0.1 s as in the present reference book 1.

Exellent period determination of seismic waves

In the study of seismic wave characteristics, the frequency characteristic, often referred to as the excellent period, is a crucial parameter. This period represents the point at which the power spectrum of the seismic wave reaches its peak, providing essential insights into the wave's potential impact on structures [15] [16] [17]. Accurately determining the excellent period is vital for effective seismic analysis and design. When selecting seismic waves for time history analysis, it is important to choose waves with an excellent period that closely matches the natural vibration period of the construction site. This alignment ensures that the seismic analysis accurately reflects the site's conditions, leading to more reliable and effective aseismic design. Methods such as Fourier transform analysis are employed to precisely identify the excellent period, enhancing the accuracy of seismic response predictions. By integrating empirical data with theoretical models, this study contributes to the development of a scientifically robust dynamic coefficient β curve, ensuring its applicability in modern seismic design standards and improving the safety and resilience of structures subjected to seismic forces.

The exellent period of the seismic wave usually converts the acceleration time history data of seismic waves into Fourier transform to determine the period of the point at which the power is greatest as in Fig. 6.

Figure 6 exellent period determination of seismic waves by Fourier transform

In the case of a similar peak, such as Fig. 7, it is impossible to distinguish which is the true exellent period.

Figure 7 The output spectrum of the 1994 Northridge, Arleta and Nordthoff Fire Station 90 Deg

This shows that the problem of determining the order of exellent period of seismic waves should not be studied only by means of the "signal processing theory" or "seismic engineering" method of dealing with ordinary

time series data, but in conjunction with the "aseismic engineering" method of studying the seismic response characteristics of the structure.

The Fourier transform $X(T)$ of the time series $x(t)$ is as follows:

$$
X(T) = \int_{-\infty}^{\infty} x(t)e^{\frac{-i2\pi}{T}}dt
$$
\n(22)

In comparison with Equations (21) and (22), the difference is essentially the same and the difference is that Equation (21) contains the damping ratio ζ of the material.

In the dynamical coefficient β-T curve, the acceleration response decreases sharply at the point of exellent period.

Thus, when $\zeta = 0$, it can be speculated that the point of sharp descent in the β -T curve acceleration response spectral curve and the point of exellent period of the seismic wave obtained with the Fourier transform coincide.

Figure 8 Acceleration response spectrum of 1994 Northridge, Arleta and Nordthoff Fire Station90 Deg (damping ratio ζ=0)

In Fig. 8, it is clear that the exellent period of the seismic wave is 0.92 s.

In this way, the exellent period of the seismic wave is determined and presented in Appendix 1.

The determination of βmax

In the present study, with the results of the calculation of the damping ratio $\zeta = 0.05$ of concrete material based on the dynamical coefficient curve, β from the smallest period in which the acceleration response in the accelerometer response spectral curve was sharply increased to a period of 0.05 s to a period of sharply smaller magnitude, yielding and controlling the calculated results of 7958 points according to 72 seismic waves presented in the appendix.

The mean value of the sample $m = 2.215$ the standard deviation $S = 0.4692$.

Fig. 9 is a column diagram for estimating the probability density function of βmax when the magnitude of the class is 0.2, and a probability density function graph of the Gaussian normal distribution with mathematical meam values and standard deviation of 2.215 and 0.469.

Figure 9 Column diagram and probability density function curve of βmax

Fig. 9 shows that the distribution of βmax is very close to the normal distribution.

To confirm that the distribution of βmax is a normal distribution, a statistical hypothesis test was performed, which did not obtain the basis for acceptance as a normal distribution.

Using the normplot function of Matlab that visually shows the fitness of the normal distribution, the plot is shown as Fig. 10.

Figure 10 Fitness verification of the normal distribution for the sample sequence by normplot

Figure 10 shows that the distribution of βmax from 1.1 to 2.65, where the mean value of 2.215 belongs, depends on the normal distribution. However, since the value of βmax is above 2.65, it is shown that the sample values are rapidly departing from the normal distribution.

However, as is typically the case in experimental planning methods, it is not feasible to eliminate abnormalities using a deception test because βmax values are derived from actual seismic records. Consequently, it is unreasonable to attempt this through an angle test or by forcing the sample sequence into a normal distribution, as the actual calculation results and the statistical characteristics of the newly configured sample sequence differ from the original ones. This discrepancy arises because seismic acceleration recording is a highly irregular and abnormal random process that defies conventional pattern recognition. Therefore, we assert that a convincing βmax does not conform to a normal distribution across the entire computational value interval. However, near the mean of βmax, it is reasonable to estimate its confidence limit value.

x₁, x₂,…, xn is generally referred to as sample random variables of size n, and if n is large enough when we do not know the population squared deviation, the confidence interval of the population mean m with confidence probability p is as follows.

$$
(m - xp \cdot \frac{S}{\sqrt{n-1}}, m + xp \cdot \frac{S}{\sqrt{n-1}})
$$
\n(23)

$$
\frac{1}{\sqrt{2\pi}} \int_{0}^{x_p} e^{-\frac{z^2}{2}} dz = \frac{p}{2}
$$

Here, xp is the value of 0

$$
x0.05=2.0
$$

Estimating the confidence interval of βmax with a 95% confidence rate is as follows.

$$
\beta_{\text{max}} = (2.215 - 2.0 \cdot \frac{0.469}{\sqrt{7957}}, 2.215 + 2.0 \cdot \frac{0.469}{\sqrt{7957}}) =
$$

= (2.205 ~ 2.225)

Thus, βmax=2.2

Decision of the descent interval of βmax

As the lower limit value in Reference 1 is (Tg/T) 0.9βmax=0.2βmax, Fig. 1 equals Fig. 11.

That is, the dynamical coefficient curve from 6Tg becomes the horizontal line again.

Figure 11 The dynamical coefficient β curve redrawn Fig. 1

On the other hand, in almost every country's aseismic design standard, for example, if it descends into (Tg/T) fractional function as in Fig. 3, the dynamical coefficient curve becomes a horizontal line again at 5Tg.

This is, after all, that the bifurcation point of the 1/T descent region of the dynamical coefficient beta curve is at 5Tg to 6Tg.

In the present study, considering the results, the acceleration response spectral curve descends to a 1/T function up to its median 5.5 Tg. However, as shown in Appendix 1, the curve continues to descend as the natural vibration period of the structure increases. Therefore, in Figures 2 and 3, unlike Figure 1, there is no horizontal interval in the acceleration response spectral curve. The dynamic coefficient curve descends in two ways: first, it descends to the hyperbolic form of a fractional function, as seen in UBC 97, where a relatively long natural oscillation period results in an excessively small acceleration response, weakening structural safety. Second, the descending section is divided into two parts, initially descending to a 1/T function and then transitioning to a 1/T² function at a branch point or to a slope, as depicted in Figures 2 and 3. This approach is scientific and reasonable because when the descending function transitions from a 1/T to a 1/T² function at a branch point, the curve is not continuous, causing a jump. This issue does not arise with an oblique straight line, as illustrated in Figure 12. In this figure, curve 1 represents the true acceleration response spectral curve, while curve 2 descends to a 1/T function, and curve 3 descends to a 1/T² function. The xcoordinate of the first starting point of descent to a 1/T² function corresponds to the excellent period of the seismic wave, with the y-coordinate at βmax, specifically 2.225. In the example of the 1952 Hollywood Storage P.E 270 Deg seismic waves and Appendix 2, it is evident that descending to a $1/T$ function and then to a $1/T²$ function is inaccurate for almost every β-curve seismic wave. The seismic waves with a real acceleration response greater than $(1/T²)$ ·βmax in the interval after the excellent period are listed in Table 1. This analysis confirms that it is not safe to define the second interval function of the descending interval as a 1/T² function. Instead, by descending almost all seismic waves into a 1/T function to a branch point and then transitioning to a slope line, as shown in Figure 2, we can safely reflect the true acceleration response.

This problem is not raised by the oblique straight line.

Let's see Fig. 12.

In Fig. 12, curve 1 is the true acceleration response spectral curve and curve 2 is a curve that descends to a 1/T function.

Figure 12 Dynamic coefficient β curve based on the results of the previous study

Curve 3 is a curve that descends to a 1/T2 function; the x coordinates of the first starting point, which descended to a 1/T2 function descending to a 1/T function, are the exellent period points of the corresponding seismic wave, and the y coordinates are βmax, in detail, 2.225.

Figure 13 Accelerated response spectral curves of 1952 Hollywood Storage P.E 270

In the 1952 Hollywood Storage P.E 270 Deg seismic waves of the example, and Appendix 2, it can be seen that it is inaccurate to see that it descends to a 1/T function to a point of a period at almost every β-curve seismic wave and then descends to a 1/T2 function.

The seismic waves with a real acceleration response greater than (1/T2)·βmax in the interval after the exellent period are the same as Table 1.

Seeing Table 1 and Appendix 2, 30 seismic waves close to nearly half of the 72 seismic waves collected were confirmed that the values of the acceleration response spectra in the period interval up to 10 s currently calculated were significantly greater than the function values of 1/T2.

The remaining 42 seismic waves were found to be very close to the 1/T2 function values in a relatively long period, but by no means less than 1/T2 the value of the acceleration response spectrum.

Therefore, we can conclude that it is not safe to catch the second interval function of the descending interval as a 1/T2 function.

In Appendix 2, it is concluded that by descending almost all seismic waves into a function of 1/T to a branch point and then taking a descending function in a slope line, as shown in Figure 2, we can safely reflect the true state of the acceleration response. Here, the lower limit value of the dynamic coefficient β curve is determined statistically from the calculated results when $T = 10$ seconds. The finishing period of foreign aseismic standards is usually between 3 to 4 seconds, and considering a period of 6 seconds along with the natural vibration period calculation results of actual structures, we can utilize the values of the dynamic coefficients in real and scientific research. The value of the acceleration response spectrum when $T = 10$ seconds is expressed as a ratio of βmax, rather than an absolute value. The mean value of the acceleration response spectrum at 72 seismic waves at $T = 10$ seconds is 0.08632, with a standard deviation of 0.1325, and 0.0388 β max, with a standard deviation of 0.05956βmax. The detailed calculation results are presented in Appendix 1. Now, let us estimate the value of the lower limit with a 95% confidence rate, similar to the estimation of βmax. The confidence interval of the lower limit value of the acceleration response spectrum is estimated as follows with a 95% confidence rate: $(0.05294\beta \text{max} \sim 0.02467\beta \text{max})$. Thus, from a safety perspective, the lower limit value is 0.05294βmax. Since the branching point value is 5.5 Tg, we take the descending shape into the slope line

after the bifurcation point as follows: $\beta = [a - b(T - 5.5Tg)]$ ·βmax. By substituting the boundary conditions when $T = 5.5$ Tg and $T = 10$ seconds, and considering Tg to be 0.1 seconds for safety, we determine the values of a and b in Equation 18 to be 0.18 and 0.0135, respectively. The result is equal to Equation 19: $\beta = [0.18 - 1.000]$ $0.0135(T - 5.5Tg)$]·βmax. Thus, finally, the dynamic coefficient β is determined as shown in Figure 14, with βmax being 2.2, as previously established.

The confidence interval of the lower limit value of the acceleration response spectrum is estimated as follows with 95% confidence rate.

$$
(0.0388 - 1.96 \cdot \frac{0.05956}{\sqrt{71}}, 0.0388 + 1.96 \cdot \frac{0.05956}{\sqrt{71}})\beta_{\text{max}}
$$

= (0.02467 ~ 0.05294)\beta_{\text{max}}

Thus, from the point of view of safety, the lower limit value is 0.05294βmax.

Since the branching point value is 5.5 Tg, let's take the descending shape into the slope line after the bifurcation point as follows.

 $β=[a-b(T-5.5Tg)]$ ·βmax (24)

If we look at Equation 18, we need to obtain a, b by substituting the boundary conditions when $T=5.5$ Tg and when $T=10$ s.

By the way, Tg is unknown.

The smaller the value of Tg, the safer the value of b.

Therefore, we determined the value of Tg to be 0.1 s which could be the lowest and the a and b of Equation 18 to 0.18 and 0.0135, respectively.

The result is equal to Equation 19.

$$
\beta = [0.18 - 0.0135(T - 5.5Tg)] \cdot \beta \text{max} \tag{25}
$$

Thus, finally, the dynamical coefficient β is determined as Fig. 14.

βmax is 2.2, as we have seen before.

Figure 14 The newly proposed dynamical coefficient β curve

4. Conclusions

Based on the insights gained from this study, we conclude that representing the acceleration response as a multiple of βmax when $T = 0$ is inaccurate; instead, it is correct to represent β as 1.0. The dynamic coefficient curve, which descends to a 1/T fractional function and then transitions into an oblique straight line, is scientifically robust and offers superior safety compared to descending to a $1/T²$ function. This approach provides a more accurate representation of the acceleration response, particularly for structures with longer natural vibration periods. In determining the excellent period of seismic waves, it is argued that this can be achieved more precisely by combining acceleration response spectral values rather than relying solely on Fourier spectral values. The proposed dynamic coefficient curve, as illustrated in Figure 13, is both scientific and reliable, serving as a solid foundation for elastic response spectral analysis and demand spectrum

methodologies, particularly in the context of buildings with relatively large natural vibration periods. This study contributes to enhancing the accuracy and applicability of seismic design standards, ensuring improved structural resilience against seismic forces.

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6. Conflict of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper. All authors have approved the final version of the manuscript and agree with its submission to the International Journal of Architecture and Urbanism.

Reference

- [1] Song Chon Choi (2010), The Aseismic Structural Design Standards for Building, The Ministry of Management of State Construction: 20–32
- [2] GB 5011-2010(2010), Building Aseismic Design Code, Unity Training Course, Earthquake Press: 51– 65
- [3] Tan Wenhui and Li Da, High-rise building structure design,YeJin Indastrial press 2013. 80–90
- [4] E. Kurbatsky dan V. Mondrus, "Dynamic Coefficients or Response Spectra of Structures to Earthquake?," Scientific journal "ACADEMIA. ARCHITECTURE AND CONSTRUCTION", vol. 2019, 2019. [Online].
- [5] M. Pehlivan, E. Rathje, dan R. Gilbert, "Factors influencing soil surface seismic hazard curves," Soil Dynamics and Earthquake Engineering, vol. 83, pp. 180-190, 2016. [Online].
- [6] F. Behnamfar dan A. Fathollahi, "Conversion factors for design spectral accelerations including soil– structure interaction," Bulletin of Earthquake Engineering, vol. 14, pp. 2731-2755, 2016. [Online].
- [7] M. Al-Ansari, "Reliability Index of Tall Buildings in Earthquake Zones," OJER, vol. 2, no. 3, pp. 39-46, 2013. [Online].
- [8] F. Sardari, M. R. Dehkordi, M. Eghbali, dan D. Samadian, "Practical seismic retrofit strategy based on reliability and resiliency analysis for typical existing steel school buildings in Iran," International Journal of Disaster Risk Reduction, vol. 51, pp. 101890, 2020. [Online].
- [9] N. Lagaros, A. Th. Garavelas, dan M. Papadrakakis, "Innovative seismic design optimization with reliability constraints," Computer Methods in Applied Mechanics and Engineering, vol. 198, pp. 28-41, 2008. [Online].
- [10] C. Fang dan W. Wang, "Structural Responses: Single-Degree-of-Freedom (SDOF) Systems," Shape Memory Alloys for Seismic Resilience, Springer, 2019. [Online].
- [11] E. Bojórquez, J. Bojórquez, S. Ruiz, A. Reyes-Salazar, dan J. I. Velazquez-Dimas, "Response transformation factors for deterministic-based and reliability-based seismic design," Structural Engineering and Mechanics, vol. 46, no. 6, pp. 755-773, 2013. [Online].
- [12] F. Graziotti, A. Penna, dan G. Magenes, "A nonlinear SDOF model for the simplified evaluation of the displacement demand of low-rise URM buildings," Bulletin of Earthquake Engineering, vol. 14, no. 6, pp. 1589-1612, 2016. [Online].
- [13] J. Karapetyan, "Comparative analysis of dynamic coefficient β(T, n) curves obtained by different methods," Seismic Instruments, vol. 49, pp. 307-314, 2013. [Online]. Available: https://consensus.app/papers/analysis-coefficient-curves-obtained-methodskarapetyan/f61ec172708e5a74b3fa928147d5a40e/?utm_source=chatgpt.
- [14] K. Kawashima dan K. Aizawa, "MODIFICATION OF EARTHQUAKE RESPONSE SPECTRA WITH RESPECT TO DAMPING," Doboku Gakkai Ronbunshu, vol. 1984, pp. 351-355, 1984. [Online]. Available: [https://consensus.app/papers/modification-earthquake-response-spectra-with-respect](https://consensus.app/papers/modification-earthquake-response-spectra-with-respect-kawashima/8509eadc8ab05cd482a59e1b108e1538/?utm_source=chatgpt)[kawashima/8509eadc8ab05cd482a59e1b108e1538/?utm_source=chatgpt.](https://consensus.app/papers/modification-earthquake-response-spectra-with-respect-kawashima/8509eadc8ab05cd482a59e1b108e1538/?utm_source=chatgpt)
- [15] Z. Yongfeng dan T. Gengshu, "An Investigation of Characteristic Periods of Seismic Ground Motions," Journal of Earthquake Engineering, vol. 13, pp. 540-565, 2009. [Online]. Available: https://consensus.app/papers/investigation-characteristic-periods-seismic-groundyongfeng/3762dd2ed3cb52f0b7fb557424b533c3/?utm_source=chatgpt.
- [16] G. Chen, X. Ning, H. Guo, dan H. Zhou, "Characteristic Analysis of 3.11 Seismic Waves," Advanced Materials Research, vol. 838-841, pp. 1484-1491, 2013. [Online]. Available: https://consensus.app/papers/analysis-seismic-waveschen/8b69aad6e23b5b748729205a9a5e6f11/?utm_source=chatgpt.
- [17] Q. Bai, F. Zhu, Y. Kang, dan J. Bian, "Power spectral density estimation of seismic wave based on wavelet transform," 2008 Chinese Control and Decision Conference, pp. 4600-4603, 2008. [Online]. Available: [https://consensus.app/papers/power-density-estimation-wave-based-wavelet-transform](https://consensus.app/papers/power-density-estimation-wave-based-wavelet-transform-bai/d822565c3e3d51cc8ebeabda8897e670/?utm_source=chatgpt)[bai/d822565c3e3d51cc8ebeabda8897e670/?utm_source=chatgpt.](https://consensus.app/papers/power-density-estimation-wave-based-wavelet-transform-bai/d822565c3e3d51cc8ebeabda8897e670/?utm_source=chatgpt)

Table Characteristics of seismic acceleration records

Appendix 2

In the figures of Appendix 2, curve 1 is the acceleration response spectral curve, curve 2 is a curve that descends to a 1/*T* function, and curve 3 is a curve that descends to a $1/T²$ function.

15. 1971 San Fernando Pocoima Dam 196 Deg

31. 1995 HYOGOKEN-South, N12W

39. HOLLISTER-SOUTH STREET AND PINE DRIVE AT 90 Deg

40. CENTURY CITY-LACC NORTH AT 0 Deg

55. SYLMAR-COUNTY HOSP PARKING LOT AT 90 Deg

56. YERMO-FIRE STATION AT 0 Deg

Unknown recording Station